

## Worksheet

### Exercise 1

- Determine the formula for the  $n$ th term of the following arithmetic sequences.
  - 1.1  $-2; 5; 12; 19; \dots$
  - 1.2  $3; 1; -1; -3; \dots$
  - 1.3  $7; 11; 15; 19; \dots$
  - 1.4  $4; 0; -4; -8; \dots$
- Given the sequence  $4; 10; 16; \dots$ 
  - 2.1 Write down the next 3 terms.
  - 2.2 Determine the general formula  $T_n$ .
  - 2.3 Calculate  $T_{14}$ .
  - 2.4 Which term has a value of 70?
- Given the sequence  $18; 13; 8; \dots$ 
  - 3.1 Write down the next 3 terms.
  - 3.2 Determine the general formula  $T_n$ .
  - 3.3 Calculate  $T_{15}$ .
  - 3.4 Which term has a value of  $-37$ ?
- Calculate the number of terms in the sequence  $301; 297; 293, \dots; -15$
- The fourth term of an arithmetic sequence is 55 and the tenth term is 45. Calculate the value of  $T_{37}$ .
- The first three terms of an arithmetic sequence are  $2k + 7, 4k + 1; 5k - 1$ . Calculate the value of  $k$  and write down the first three terms.
- In an arithmetic sequence, the seventh term is 9 more than the fourth term. The sixth term is 5. Calculate:
  - 7.1 the first term
  - 7.2 the constant difference.
- The  $n$ th term of an arithmetic sequence is  $x$  and the  $(n + 1)$ th term is  $y$ . Find the first term of the sequence in terms of  $x, y$  and  $n$ .

### Sum of an arithmetic sequence

To find the sum of an arithmetic sequence, write it forwards and then backwards and add.

$$S = a + (a + d) + (a + 2d) + \dots (l - 2d) + (l - d) + l \quad [\text{where } l \text{ is the last term}]$$

$$S = l + (l - d) + (l - 2d) + \dots (a + 2d) + (a + d) + a$$

$$\therefore 2S = (a + l) + (a + l) + \dots \text{to } n \text{ terms} \\ = n(a + l)$$

$$\therefore S = \frac{n}{2}(a + l) \text{ or } S = \frac{n}{2}(2a + (n - 1)d)$$

### EXAMPLE

Find the sum of the terms in the series:  $53 + 49 + 45 + \dots + 9$ .

#### Solution

In the example on page 12, we calculated  $n$  to be 12. There are 12 terms in the series.

Using the formula:  $S = \frac{n}{2}(a + l)$

$$S_{12} = \frac{12}{2}(53 + 9) = 372$$

Using the formula:  $S = \frac{n}{2}(2a + (n - 1)d)$

$$S_{12} = \frac{12}{2}(2(53) + (12 - 1)(-4)) = 372$$

### Exercise 2

- Calculate the sum of the arithmetic series:  $4 + 7 + 10 + \dots + 751$ .
- Find the sum of the first 11 terms of the series with  $T_n = 5n - 3$ .
- The sum to  $n$  terms of an arithmetic series is  $S_n = \frac{n}{2}(7n + 15)$ .
  - 3.1 How many terms must be added to give a sum of 425?
  - 3.2 Determine the 10th term of the series.