Worksheet 1

The parabola

1. Rewrite each equation in standard form $y = ax^2 + bx + c$ and identify the values of a, b and c.

1.1
$$y = 2(x-1)^2 + 3$$

1.2
$$f(x) = -(x-1)^2 + 12$$

1.3
$$y = a(x - p)^2 + q$$

2. Rewrite each of the following in turning point form $y = a(x - p)^2 + q$. Identify the value of *a*, *p* and *q*.

2.1
$$y = 2x^2 + 2x + 1$$

2.2
$$g(x) = 3x^2 + 3x$$

2.3
$$f(x) = ax^2 + bx + c$$

3. Make a sketch of each equation. Clearly indicate the turning point and show the axis

3.1
$$y = (x-2)^2 + 3$$

3.2
$$y = -7(x+2)^2 - 7$$

$$3.3 y = x^2 + 6x + 5$$

4. Determine the range and domain of each function in question 3.

4.1
$$y = (x-2)^2 + 3$$

4.2
$$y = -7(x+2)^2 - 7$$

4.3
$$y = x^2 + 6x + 5$$

5. Draw a rough sketch graph of a parabola using the following information.

5.1
$$a > 0$$
, $r_1 < 0$ and $r_2 > 0$

5.2
$$a > 0$$
, the graph reaches a minimum at (2; 1)

5.3
$$a < 0, r_1 = r_2 = 4$$

6. Determine whether each equation has one root, two roots or no roots.

6.1
$$y = 3x^2 + 2x$$

6.2
$$f(x) = (x+1)^2 + 2$$

6.3
$$g(x) = 3(x-2)(x+2)$$

6.4
$$h(x) = ax^2 + bx + c$$
 where $4ac = -1$

The hyperbola

1. Sketch the graph of each function on a separate axis. Clearly indicate the asymptotes and intersection points with the axes, if any.

1.1
$$y = \frac{2}{x}$$

1.2
$$y = \frac{1}{x} - 1$$

1.3
$$y = \frac{x^{3}}{x-3} + 2$$

2. Use your sketches in question 1 to determine the range and domain for the following.

2.1
$$y = \frac{2}{x}$$

2.2
$$y = \frac{1}{x} - 1$$

2.1
$$y = \frac{2}{x}$$

2.3 $y = \frac{-3}{x-3} + 2$

3. If A is the point of intersection of the asymptotes, determine the value of the hyperbolic function $y = \frac{a}{x - p} + q.$

3.1
$$A = (3; 1)$$
 and $a = 1$

3.2 A = (0; 0) and
$$a = -1$$

3.3 A =
$$(-1; -1)$$
 and $a = 3$

3.4
$$A = (0; 3)$$
 and $a = 2$

3.5 A =
$$(-1; 0)$$
 and $a = -2$

4. Determine the lines of symmetry of each function.

4.1
$$y = \frac{1}{x}$$

4.2
$$y = \frac{1}{x} - 2$$

4.3
$$y = -\frac{1}{x} + 3$$

4.2
$$y = \frac{1}{x} - 2$$

4.4 $y = \frac{3}{x+2} + 4$

4.5 $y = \frac{4}{x-3} - 2$

may not be reproduced.